Restoration of fMRI Decodability Does Not Imply Latent Working Memory States

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Abstract

■ Recent imaging studies have challenged the prevailing view that working memory is mediated by sustained neural activity. Using machine learning methods to reconstruct memory content, these studies found that previously diminished representations can be restored by retrospective cueing or other forms of stimulation. These findings have been interpreted as evidence for an activity-silent working memory state that can be reactivated dependent on task demands. Here, we test the validity of this conclusion by formulating a neural pro-

cess model of working memory based on sustained activity and using this model to emulate a spatial recall task with retrocueing. The simulation reproduces both behavioral and fMRI results previously taken as evidence for latent states, in particular the restoration of spatial reconstruction quality following an informative cue. Our results demonstrate that recovery of the decodability of an imaging signal does not provide compelling evidence for an activity-silent working memory state.

INTRODUCTION

The dominant view of the neural mechanism underlying working memory is that memory representations are maintained in the sustained spiking activity of neurons (Chaudhuri & Fiete, 2016; Bays, 2015; Eriksson, Vogel, Lansner, Bergström, & Nyberg, 2015; Funahashi, Bruce, & Goldman-Rakic, 1989; Fuster & Alexander, 1971). This sustained activity may arise from local self-excitation in populations of neurons or reverberatory loops between different cortical areas (Wang, 2001). Working memory representations can be modeled as attractor states in the neural activation dynamics. For continuous features, such as location, color, or orientation of visual stimuli, population codes with homogeneous recurrent connectivity form continuous attractors such that each possible feature value can be maintained in working memory (Johnson, Simmering, & Buss, 2014; Wei, Wang, & Wang, 2012; Compte, Brunel, Goldman-Rakic, & Wang, 2000). Errors arise at encoding and when the attractors drift to neighboring feature values or decay under the influence of random noise (Wimmer, Nykamp, Constantinidis, & Compte, 2014; Burak & Fiete, 2012; Camperi & Wang, 1998).

Models of this type have successfully accounted for memory-related neural activity at a high level of physiological detail (Wimmer et al., 2014; Compte et al., 2000). In addition, they have been used to explain a wide range of behavioral findings, such as performance and capacity limits in change detection tasks (Engel & Wang, 2011; Johnson, Spencer, & Schöner, 2009), biases in visual working memory (Schneegans, Spencer, Schöner, Hwang, & Hollingworth, 2014; Simmering, Spencer, & Schöner, 2006; Camperi & Wang, 1998), and developmental changes in working memory performance (Schutte & Spencer, 2009; Edin, Macoveanu, Olesen, Tegnér, & Klingberg, 2007).

A strikingly different account of working memory proposes that memory representations are maintained in an activity-silent state (i.e., without sustained neural firing) through biochemical or morphological changes in neurons (Stokes, 2015; Barak & Tsodyks, 2014). A prominent candidate mechanism is rapid synaptic plasticity (Erickson, Maramara, & Lisman, 2010), which may allow sensory stimulation to produce changes in neural connection patterns over short timescales and create assemblies of neurons that may later be reactivated by nonspecific input (Mi, Katkov, & Tsodyks, 2017; Mongillo, Barak, & Tsodyks, 2008). Proponents of such working memory mechanisms suggest that persistent neural activity only reflects sustained attention to the currently taskrelevant item, whereas other items can be held in an activity-silent state (Rose et al., 2016; LaRocque, Lewis-Peacock, Drysdale, Oberauer, & Postle, 2013; Lewis-Peacock, Drysdale, Oberauer, & Postle, 2012).

An important source of information about the neural basis of working memory is provided by fMRI studies that measure neural activity during the delay periods of working memory tasks. Results of early studies were consistent with the sustained firing account, finding elevated BOLD signals in regions of prefrontal and parietal cortex University of Cambridge **Example 2004** (Xu & Chun, 2006; Todd & Marois, 2004; Linden et al.,

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2003; Courtney, Ungerleider, Keil, & Haxby, 1997). However, the interpretation of these univariate fMRI results is not necessarily straightforward. More recent studies have applied multivariate pattern analysis and reconstruction methods to BOLD signal data to characterize working memory representation (Sprague, Ester, & Serences, 2014; Riggall & Postle, 2012; Harrison & Tong, 2009; Serences, Ester, Vogel, & Awh, 2009). Such studies have found a dissociation between cortical regions with elevated BOLD signal and regions from which the features of remembered items could be successfully decoded (Emrich, Riggall, LaRocque, & Postle, 2013; Riggall & Postle, 2012).

Recently, such reconstruction methods have also been used to investigate how working memory representations change when informative cues are provided during the delay period. In the task used by Sprague, Ester, and Serences (2016), participants had to memorize the locations of two colored disks. In some trials, a color cue given midway through the memory period indicated which location would be tested at the end. The reconstruction quality for the cued item's location decreased over the course of the delay period but showed a significant restoration following this spatially nonspecific retro-cue. This was interpreted as evidence for an activitysilent component in location working memory, which cannot be decoded from the BOLD signal data but can be reactivated (and thereby contribute to reconstruction quality again) by the retro-cue.

Similar conclusions have been drawn from several prominent studies applying reconstruction methods to fMRI and EEG data. Rose et al. (2016) found that the category of a currently task-relevant item could be successfully decoded from fMRI recordings, but not the category of a second item concurrently held in working memory (that became task relevant at a later stage). The authors concluded that this second item is held in an activitysilent state and is only restored into a sustained activity representation when cued as immediately task relevant. A restoration of decoding quality from EEG data has been observed following TMS pulses (Rose et al., 2016) or presentation of salient, but uninformative, visual stimuli (Wolff, Jochim, Akyürek, & Stokes, 2017; Wolff, Ding, Myers, & Stokes, 2015). This was interpreted as effect of interactions between the unspecific stimulation and a silent working memory representation, realized in a changed neural connectivity pattern.

In this study, we critically examine the interpretation that the restoration of reconstruction quality following a cue is evidence for activity-silent working memory states. We implement a neural model of working memory based on the principle of sustained activity through selfexcitation in neural populations and derive simulated BOLD signal data from this model. We then apply the same kind of reconstruction method as was previously used for the analysis of experimental data. Focusing on the study by Sprague et al. (2016), we demonstrate that the neural model can reproduce both the behavioral and fMRI reconstruction results, despite relying only on active memory representations. In particular, in a minimal neural model of the retro-cue task, a spatially nonspecific color cue can selectively strengthen the reconstruction of the cued item's location. The neural model demonstrates that the assumption of activity-silent WM states is not necessary to explain these experimental results and highlights the importance of considering the functional neural architectures involved in the task when interpreting imaging data.

METHODS

Neural Model

We aim to provide a minimal neural model that can perform the delayed estimation task with retro-cueing (Figure 1A) and account for the behavioral and fMRI results from the experimental study of Sprague et al. (2016). We formulate this model within the framework of dynamic neural fields, a form of recurrent neural network that describes the continuous evolution of activity distributions in neural populations through differential equations (Schneegans & Schöner, 2008). Neural fields are continuous in space: Rather than simulating the activity of individual neurons, each point in a neural field reflects the mean activity of neurons with the corresponding spatial selectivity. Working memory is realized in this framework through localized peaks of activation that are sustained through self-excitation (balanced by surround inhibition), forming attractor states in the neural dynamics. Neural field models generate continuous time courses of neural activity patterns, making them well suited for modeling fMRI data (Wijeakumar, Ambrose, Spencer, & Curtu, 2016).

We employ a single combined perceptual and working memory representation to emulate neural activation in the task (Figure 1B). Stimulus locations are represented in a population code over 2-D visual space. Importantly, the model also needs to represent the item color associated with each location to select the correct memorized item for response following a color cue. Following a recent model of feature binding in visual working memory, we employ a conjunctive code for color–location bindings (Schneegans & Bays, 2017; Schneegans, Spencer, & Schöner, 2016). To keep the model simple, we represent only the two stimulus colors used in the original experiment (red and blue), yielding two neural fields for these discrete colors over the same 2-D visual space. These can be interpreted as slices from a full population code for possible color–location conjunctions (compare Richter, Lins, Schneegans, & Schöner, 2014; Lipinski, Schneegans, Sandamirskaya, Spencer, & Schöner, 2012).

The activation in these fields, which can be equated with the mean membrane potential of neurons with the

Figure 1. (A) Experimental task of Sprague et al. (2016). Participants view a sample array of two colored discs and have to report the location of one item (the target) by adjusting a vertical or horizontal bar (yellow arrows are not part of the experimental display). The color of the fixation point can change at different times during the delay period to indicate the target item. (B) Architecture of the neural model. Two neural fields over retinal space, with selectivity matching the two colors (blue and red) used in the task, are shown as color-coded activation distributions. Each colored sample stimulus provides localized input to the corresponding field, generating a peak of activity that encodes the stimulus location. The informative color cue generates a homogeneous input to the field of matching color, boosting activity throughout the population.

corresponding selectivity (Amari, 1977), is governed by the differential equation

$$
\begin{aligned} \tau \dot{a}(l, \mathbf{x}, t) &= -a(l, \mathbf{x}, t) + b + s(l, \mathbf{x}, t) + g(l, \mathbf{x}, t) \\ &+ \xi(l, \mathbf{x}, t) \end{aligned} \tag{1}
$$

where $a(l, \mathbf{x}, t)$ is the activation for color $l \in \{ \text{red}, \text{blue} \},$ spatial position $\mathbf{x} = (x, y)$, and time t. The notation \dot{a} indicates the rate of change of activation over time, with a time constant τ . The scalar variable *b* is the global resting level of activation that the field will relax to in the absence of input and lateral interactions, s is the local external input to each field location, g is the input from lateral

interactions within the model, and ξ is a random noise term.

The lateral interactions are based on the current field output, a continuous homologue of the neural firing rate, which is computed from the activation a via a sigmoid (logistic) function f:

$$
f(a) = \frac{1}{1 + e^{-a}}\tag{2}
$$

The output is close to zero for low (negative) activation values, rises for activation values around zero, and saturates at a value of one for higher activations. This produces the effect that only regions with high activation contribute to interactions within the field.

Lateral interactions consist of three components: a local excitatory component, described by a normalized 2-D Gaussian function $\phi(\mathbf{x}; \sigma_{\text{exc}})$ with mean zero and width parameter σ_{exc} that is scaled with an excitatory weight $c_{\rm exc}$; a uniform inhibitory component within each color field with weight c_{inhc} ; and a global inhibitory component over both fields with weight c_{inhg} . The input from lateral interactions for each field position is computed as

$$
g(l, \mathbf{x}, t) = \int f(a(l, \mathbf{x}', t))(c_{\text{exc}}\phi(\mathbf{x} - \mathbf{x}'; \sigma_{\text{exc}}) - c_{\text{inhc}})(3)
$$

$$
d\mathbf{x}' - c_{\text{inhg}}\sum_{l'}\int f(a(l', \mathbf{x}', t)) d\mathbf{x}'
$$

The noise term ξ describes spatially correlated random noise with amplitude c_{noise} , generated from white noise by convolution with a Gaussian kernel (using the same width parameter σ_{exc} as in the lateral interactions):

$$
\xi(l, \mathbf{x}, t) = c_{\text{noise}} \int v(l, \mathbf{x}', t) \phi(\mathbf{x} - \mathbf{x}'; \sigma_{\text{exc}}) d\mathbf{x}', \tag{4}
$$

$$
v(l, \mathbf{x}, t) \sim \mathcal{N}(0, 1)
$$

Model parameters were adjusted manually to produce a close fit to the behavioral and fMRI reconstruction data and are fixed across task conditions. All parameter values are listed in Table 1. The model was simulated numerically by sampling the visual space in the range $[-6^\circ, 6^\circ] \times$ $[-6^\circ, 6^\circ]$ with 100 × 100 sampling points and approximating the temporal evolution of activation using the Euler method with a fixed time step of 10 msec.

Behavioral Task and Emulation in the Model

We use the neural model to emulate the delayed estimation task used by Sprague et al. (2016), shown in Figure 1A. Participants had to memorize the locations of two colored discs (one red and one blue, diameter 0.15°) presented for 500 msec. The discs were located on an invisible circle (radius 3.5°) around a central fixation point, offset from each other by $\pm 60^{\circ}$, $\pm 120^{\circ}$, or 180°. An additional small trial-to-trial variation of relative positions was introduced by adding a random value uniformly distributed in [−0.3°, 0.3°] independently to each horizontal and vertical stimulus position. Participants had

Table 1. Parameter Values for Neural Model and Generation of Simulated BOLD Signals

Parameter	Description	Value
T	Time constant of neural dynamics	100 msec
h	Field resting level	-5
$c_{\rm exc}$	Lateral excitatory weight	20
$\sigma_{\rm exc}$	Width of lateral excitation	0.25°
c_{inhc}	Inhibitory weight (within color field)	2.6
c _{inhg}	Inhibitory weight (global)	0.52
C_{noise}	Noise amplitude	55
$C_{\rm{stim}}$	Stimulus amplitude	50
σ_{stim}	Stimulus width	2°
$c_{\rm cue}$	Color cue amplitude	17.5
c_{forget}	Deactivation amplitude after trial	5
$\sigma_{\rm vox}$	Voxel range parameter	1.5
c_{nvox}	Voxel noise amplitude	2.5

to remember stimulus locations over a delay interval of 16 sec in total, then report the location of one stimulus cued by its color.

Memory load in this task was manipulated across three conditions: In the "remember one" condition (R1), the fixation point changed color to either red or blue immediately after offset of the sample stimuli, indicating with 100% reliability which item was to be tested. The fixation point then changed to a neutral color (black) after 8 sec. In the "remember two" condition, the color of the fixation point changed to purple at the beginning of the delay period, indicating that either item could be tested. After 8 sec, the fixation point's color then either changed to black (R2-neutral), or it changed to one of the item colors, acting as a retro-cue that indicated the item to be tested with 100% reliability (R2-valid). In all conditions, the fixation point took the color of the tested item at the beginning of the response period (after the 16-sec delay). The participant then had to adjust either a horizontal or vertical line displayed on the screen to report the horizontal or vertical location of the cued item.

In the neural model, memory sample stimuli are emulated as (nonnormalized) Gaussian inputs (with amplitude c_{stim} and width parameter σ_{stim}), centered at the stimulus location \mathbf{m}_l for a stimulus with color *l*. The input for each colored stimulus only drives activation in the field for the matching color and remains active for a 500-msec interval $[t_{on}, t_{off}]$:

$$
s(l, \mathbf{x}, t) = c_{\text{stim}} \exp\left(-\frac{\|\mathbf{x} - \mathbf{m}_l\|^2}{2\sigma_{\text{stim}}^2}\right) \text{ for } t_{\text{on}} \le t \le t_{\text{off}}
$$
\n(5)

The informative color cue is modeled as a homogeneous "boost" input with amplitude c_{cue} to the field with matching color l_{cue} that is active for 500 msec after onset of the cue (see Lipinski et al., 2012, for an analogous mechanism at the perceptual level):

$$
s(l_{\text{cue}}, \mathbf{x}, t) = c_{\text{cue}} \text{ for } t_{\text{cue}} \le t \le t_{\text{cue}} + 500 \text{ msec} \quad (6)
$$

Behavioral results in retro-cue experiments indicate that processing of a retro-cue takes about 300–500 msec (Souza & Oberauer, 2016; Souza, Rerko, & Oberauer, 2014; Tanoue & Berryhill, 2012), and we assume that the cue has no further effect after this, even though it remains visible. The uninformative cues (black or purple) are not modeled explicitly.

For the generation of the spatial response in the model, the response color cue input is presented for 500 msec in the same fashion as described above and 500 msec after the offset of the cue; the spatial center of mass (x_{resp}) , y_{resp}) of the field outputs (summed over colors) is determined as

$$
x_{\text{resp}} = \frac{\sum_{l} \int x f(a(l, \mathbf{x}, t)) d\mathbf{x}}{\sum_{l} \int f(a(l, \mathbf{x}, t)) d\mathbf{x}} \tag{7}
$$

$$
y_{\text{resp}} = \frac{\sum_{l} \int y f(a(l, \mathbf{x}, t)) d\mathbf{x}}{\sum_{l} \int f(a(l, \mathbf{x}, t)) d\mathbf{x}}
$$

Note that under normal conditions, there will be a peak of activation in only one of the two fields after the presentation of the response cue (with low homogeneous activity in the other field), so this method yields the estimated location of the cued item. Response error is determined as absolute deviation of the report location from the location of the cued stimulus, either in the horizontal or vertical direction (randomly selected) to emulate the experimental response procedure. After response generation, the activation levels of both fields are transiently decreased by a value c_{forget} for 500 msec (starting 500 msec after response time) to extinguish any existing activation peaks.

We numerically simulated 10 blocks of 216 trials (72 trials per condition) of this task, with trials in each block fully counterbalanced for possible stimulus positions, angular distance between stimuli, and cued item color. Stimulus parameters directly emulate the original study, and the total number of trials approximates the number of trials across participants in that study.

In the original fMRI study, an additional mapping task was performed as basis for the reconstruction of spatial representations from voxel BOLD signals. In this task, participants memorized the location of a single stimulus, then a flickering checkerboard disc (radius 1.083°) was presented for 3000 msec, covering the location of the

memory stimulus. After this presentation, a probe stimulus was shown, and participants had to report whether the memorized stimulus location was to the left or right (or above or below) the probe. The checkerboard stimulus was shown in 36 locations on a hexagonal grid, which was again rotated in 12 different ways across sessions.

We emulate the checkerboard stimulus as a Gaussian input with the same amplitude c_{stim} and width σ_{stim} as the stimuli in the main task that is applied to the same location in the fields for both colors. We do not emulate the working memory component of the mapping task, because the simple model architecture does not allow differentiation between perceptual and working memory items. This does not affect the reconstruction procedure, because only the checkerboard stimulus locations were taken into account for computing the reconstructions in the original study. We performed four sets of this mapping task for each block of working memory trials, rotating the hexagonal stimulus grid by increments of 15° across sets and by increments of 5° across blocks.

Generating Simulated BOLD Signals

The original study measured BOLD signals for individual voxels and used an additional localizer task to assign these voxels to different cortical areas of interest (including V1, V3A, IPS0, IPS2, and sPCS). We do not aim to capture this division into different cortical regions in the model and only generate a single set of BOLD signals to compare it to the combined results from the fMRI study (which contains all of the key effects reported in that study).

The interpretation of the original study's fMRI results as evidence for activity-silent working memory is based on the assumption that the BOLD signal reflects neural spiking activity. We follow this assumption here and derive the simulated BOLD signal directly from the field output in the neural model (the continuous homologue of the firing rate). We note that this is most likely an oversimplification, but we believe that it allows the most direct test of the conclusions drawn from the original study. We define a simulated voxel by selecting a random sample of points from the two fields, $\{(l_1, \mathbf{x}_1), \ldots,$ (l_n, \mathbf{x}_n) . Building on the assumption that the visual areas under investigation are at least partly organized retinotopically, spatial locations of sampling points are drawn from a mixture of a Gaussian and a uniform distribution,

$$
p(l_i, \mathbf{x}_i) \propto 0.5 + 0.5\phi(\mathbf{x} - \mathbf{x}_{\text{vox}}; \sigma_{\text{vox}})
$$
 (8)

The center $\mathbf{x}_{\text{vox}} = (x_{\text{vox}}, y_{\text{vox}})$ of the Gaussian distribution for each voxel is chosen uniformly from the space $[-6^\circ, 6^\circ] \times [-6^\circ, 6^\circ]$ and applies to both color fields. The color l_i for each sampling point is chosen with equal probabilities from {red, blue}.

The simulated BOLD signal b for one voxel at time t_{scan} is then computed by averaging over the output signal from the neural model at these sampling points and convolving this signal in time with the canonical hemodynamic response function h :

$$
b(t_{\text{scan}}) = \int_0^\infty b(t) \frac{1}{n} \sum_i f(a(l_i, \mathbf{x}_i, t_{\text{scan}} - t)) dt + c_{\text{nvox}} \chi(t_{\text{scan}})
$$
(9)

Here, $\chi \sim \mathcal{N}(0,1)$ is random noise added to each voxel to reflect neural activity not directly related to the task. The hemodynamic response function, as defined by Lindquist, Loh, Atlas, and Wager (2009), is

$$
b(t) = \frac{t^{(\alpha_1 - 1)}\beta^{\alpha_1}e^{(-\beta t)}}{\Gamma(\alpha_1)} - c \frac{t^{(\alpha_2 - 1)}\beta^{\alpha_2}e^{(-\beta t)}}{\Gamma(\alpha_2)}
$$
(10)

with standard parameters $\alpha_1 = 6$, $\alpha_2 = 16$, $\beta = 1$, and $c = 1/6.$

Emulating the procedure in the original study, we generated BOLD signals for 10 time points in each trial of the working memory task, spaced in intervals of 2250 msec beginning at memory stimulus onset. In the mapping task, a single set of BOLD signals was generated for each trial. For each block of trials in the working memory task (and the associated trials of the mapping task), a new mapping of voxels to points in the neural fields was randomly generated. We used 1000 voxels with 1000 points per voxel. All simulated BOLD signals were transformed into z scores before further analysis, independently between blocks of trials and between mapping task and working memory task.

Reconstruction and Analysis of Spatial Representations

The reconstruction of neural representations from simulated BOLD signals is performed in the same way as the reconstruction from actual fMRI data in the original study (see Sprague et al., 2016, for details). In brief, the z-transformed BOLD signal for each voxel is modeled as a linear combination of 37 information channels (spatial filters over 2-D visual space). The data from the spatial mapping task is used to estimate a weight matrix that maps expected filter responses (based on the known stimulus locations in this task) onto the observed BOLD signals. This matrix is then inverted to compute channel activations for each trial and time point in the working memory task from measured BOLD signals.

For further analysis and visualization, reconstructed activation distributions over visual space are generated as superpositions of the spatial filters of each channel weighted with the estimated channel activation. Target positions in different trials can be aligned with each other in the reconstructions by rotating, flipping, and shifting the pattern of spatial filters associated with each channel.

To visualize and compare spatial representations over time in the different task conditions, trials are grouped by condition and absolute angular distance between memory stimuli (60°, 120°, and 180°), and reconstructions are generated, aligned with respect to the positions of the two stimuli (ignoring the small random offset in stimulus locations from trial to trial). For further analysis, trials are grouped by condition only, and reconstructions are generated, aligned by the exact location of the cued stimulus (half of the trials with a stimulus separation of 180° are omitted here to obtain equal numbers of stimulus separations −120°, −60°, 60°, 120°, and 180°). Onedimensional reconstructions over an angular space are extracted from the obtained activation distributions over visual space by interpolating and averaging activations within a ring of 2.9°–4.1° eccentricity around the center.

We apply the same analyses on these reconstructions as employed in the experimental study. A fidelity measure F of target representation in the 1-D reconstructions $r(\theta)$ (aligned with the cued stimulus position always at zero) is defined as the mean product of the reconstruction with a cosine function,

$$
F = \frac{1}{2\pi} \int r(\theta) \cos(\theta) d\theta
$$
 (11)

Activation profiles in the 1-D reconstructions are quantified by fitting with a function

$$
f(\theta) = \begin{cases} b + a \left(0.5 + 0.5 \cos \frac{2\pi |\theta - \mu|}{\sigma_{\text{fit}}} \right)^7, & \text{if } |\theta - \mu| < \sigma_{\text{fit}} \\ b, & \text{otherwise} \end{cases}
$$
(12)

where b is baseline activation, a is amplitude of a Gaussianlike component, σ_{fit} is the width parameter for this component, and μ is an angular bias of the peak limited to a small range around zero. For analysis of the model behavior, we also apply this function fitting directly to the field output in the neural model (averaged across trials, without generation of simulated BOLD signals and reconstruction from them).

To determine significance of fidelity and differences in fitting parameters, we used a bootstrapped sign test. Over 1000 iterations, we resampled with replacement from the 1-D single-trial reconstructions (with 720 trials per condition) and computed fidelity and function fit for the average over resampled reconstructions. For comparing fitting parameters between two conditions or time periods, we computed the proportion in which the difference between these variables was greater than zero and the proportion in which it was less than zero and doubled the smaller of these proportions to obtain the p value. For testing whether the fidelity measure was greater than zero, we performed a one-tailed sign test and report the proportion of resampling iterations with $F < 0$.

RESULTS

Model Mechanism and Behavioral Results

We applied a neural model of working memory based on sustained activity in neural populations to emulate the retro-cue task used by Sprague et al. (2016). In this task (Figure 1A), participants were presented with two colored disks, which they memorized in three different conditions: On R1 trials, a colored cue at the start of the trial indicated one of the items whose location was to be remembered; on R2-neutral trials, both items had to be remembered to the end of the trial; and on the critical R2-valid trials, a retro-cue delivered midway through the trial indicated which item would be tested, allowing participants to forget the other item.

The model (Figure 1B) describes activity of two spatialand color-selective populations (neural "fields") with color selectivity matching the two colors used in the task. There is localized lateral excitation within each field and global inhibition within and between fields. Figure 2 illustrates the activation time course in the model for a single trial in each task condition to demonstrate the basic mechanisms of the model. The figure shows the activation distributions in both fields at different points in time (at this stage, without generation of simulated BOLD signals or reconstructions from them).

At the beginning of the R1 trial (Figure 2A), both fields show uniformly low activation, with small fluctuations due to random noise. Presentation of the memory sample stimuli induces strong activation in both fields that is localized at the stimulus positions and specific for the color of each stimulus. Immediately following the sample stimuli, a blue color cue is presented in this trial, which homogeneously raises activation levels in the blue color field. Because of the effects of lateral interactions, this strengthens the existing peak of activation in this field, whereas activation in other parts of the field is held relatively low by the increased global inhibition arising from this peak. In addition, the global inhibitory effect acts on the activation levels in the red color field. It reduces the strength of the existing activation peak in that field such that it ceases to generate sufficient self-excitation and ultimately collapses.

After the color cue input is turned off, the activation level in the blue field decreases, but a smaller localized peak of activation remains stable throughout the delay period, sustained by local self-excitation and surround inhibition within the field. During the response period, the color cue is activated again and strengthens the remaining peak but does not qualitatively alter the activation patterns in the model. After this second cue input has ceased, the response location is determined as the center of mass of the field output over visual space (summed over both fields).

The R2-neutral trial begins in the same way as the R1 trial (Figure 2B), but here no informative color cue is given until the response period. Following the presentation of Figure 2. Evolution of activation patterns in the neural model during a single trial in each condition. Stimulus displays during different phases of the task are shown at the top of each panel. Colored bars along the time axes indicate duration of stimulus and cue inputs in the model. Activation patterns in the two fields of the model (for colors red and blue) are shown color-coded below for different points during the course of each trial.

the sample array, the activation peaks in both fields settle at a lower activation level, but they both remain stable throughout the delay period. When the color cue is presented at the end of the trial, it raises activation levels in the blue field, and the activation in the red field is suppressed through mutual inhibition. Only the activation peak for the blue item remains and forms the basis for the response generation as before.

The model simulations of the R2-valid trials combine aspects from the two previous conditions (Figure 2C). Following the presentation of the sample stimuli, local-

ized activation peaks form in both fields and remain stable during the first half of the delay period, analogous to the R2-neutral trial. When the color retro-cue is then presented, it strengthens activation in the blue field and, in turn, suppresses activation in the red field. The activation peak for the blue item then returns again to a lower activation level when the homogeneous input ceases, although it remains slightly stronger than during the first memory period because it no longer experiences inhibition from a second activation peak. The response period then proceeds in the same way as in the R1 condition.

Figure 3. Mean recall errors for different task conditions in experimental and simulation results. Boxes show 95% confidence interval based on resampling.

Figure 3 shows the mean recall errors generated by the model. The model reproduces the pattern of mean response errors in the fMRI study, with lowest errors in the R1 condition, highest in the R2-neutral condition, and intermediate in the R2-valid condition (resampling procedure producing significant difference for all pairwise comparisons, $p < .001$). Deviations of the response position from the position of the sample stimulus are generally caused by random noise in the model. Noise causes deviations between an external input and the induced activation peak during encoding and random drift in the peak location over time (Camperi & Wang, 1998). If it transiently lowers the activation level in a region by a sufficient amount, it can also cause the collapse of a peak. This is much more likely to occur when two locations are held in memory simultaneously such that the corresponding activation peaks inhibit each other. Consequently, the rate of peak collapse in the model is higher in the R2-neutral condition (21.7% of trials) than the R2-valid condition (11.6%) and the R1 condition (0%). In the case of a peak collapse, the homogeneous input for the color cue during the response phase typically induces a new activation peak at a random location, producing higher mean response errors.

Reconstruction of Spatial Representations

To compare our simulation results with the results of the fMRI study, we first generated simulated voxel BOLD signals from the output signals (homologue of neural firing rate) in the model and then performed the same reconstruction method on these simulated signals that was used for the experimental data. The generation of simulated BOLD signals and subsequent reconstructions introduces significant noise in the single trial data (compared with directly plotting the neural field activations for a trial as in Figure 2), spatial smoothing, and temporal filtering (due to the hemodynamic response function). Moreover, the purely spatial reconstruction collapses activation from the separate fields for the two colors into a single representation.

In the averaged and spatially aligned reconstructions over all trials for each condition (shown for one stimulus separation in Figure 4), the representations of stimulus locations are clearly discernible, and the reconstructions qualitatively match the activation patterns and changes over time from the fMRI study. In the R1 condition, the location of the cued and uncued stimulus can be seen with some delay after stimulus presentation (reconstruction for time point 4.5 sec), but only the location of the cued item remains active in the subsequent time points, with activation slowly diminishing over time. It should be noted that this slow decrease in activation levels does not reflect the time course in the neural model itself (where the activation levels settle into a stable state within less than one second after stimulus offset) but is created by the low-pass filter properties of the hemodynamic response function.

In the R2-neutral condition, both memory stimuli are equally represented in reconstructions throughout most of the trial, appearing with some delay after stimulus presentation and slowly diminishing in activation until the response period. The activation time course in the R2 valid condition is indistinguishable from that in the R2 neutral condition during the first half of the trial, as would be expected. After the presentation of the informative retro-cue, however, the activation increases for the location of the cued item and disappears for the location of the uncued item. This reproduces the key observation in the experimental study that a spatially uninformative retro-cue can lead to a selective strengthening of the cued item's spatial reconstruction in fMRI.

Quantitative Analysis of Reconstructions

Additional quantitative analyses are based on 1-D reconstructions of the spatial representations, which reflect activation distributions in an annulus around the fixation point. These reconstructions are aligned such that the position of the cued stimulus (the target) is always at zero and are averaged over all stimulus separations for each condition. The fidelity of target representations in these reconstructions is then determined from the concentration of activation at the target location.

The time course of target representation fidelity for the three task conditions is shown in Figure 5. Fidelity of target representation is significantly greater than zero in all conditions and for all time points starting 2.25 sec after stimulus presentation. This is to be expected given that the cued item was continuously represented as a sustained activation peak in the neural model in all trials (except for the small proportion of trials in which the peak collapsed). The fidelity time courses quantitatively reproduce the results from the experimental study. Fidelity rises sharply following the presentation of the stimulus, then decreases over time in the R1 and R2-neutral conditions, with overall higher fidelity levels in the R1 than R2-neutral condition. Critically, in the R2-valid condition, fidelity rises

Figure 4. Two-dimensional reconstructions of spatial activation patterns in the R1 condition (A), R2-neutral condition (B), and R2-valid condition (C). In each panel, the stimulus displays for different phases of the trial are shown at the top. The first row shows reconstructions from the fMRI study (Sprague et al., 2016); the second row shows reconstructions from neural model simulations.

again following the presentation of the retro-cue, reproducing this key signature of the retro-cue effect in the experimental data.

The fidelity of target representation in the simulation results also rises at the end of the trial. This is an effect of the response cue given at this time, which is realized in the same way as the retro-cue in the neural model. A rise in fidelity at the end of the trial can also be observed in the experimental results for the R1 and R2-neutral condition, although weaker than in the simulation. At least for the R2-neutral condition, we would expect that the color cue at the end of the trial should have a similar effect as a cue presented earlier. However, it is possible that, in the experimental data, there is interference in the reconstruction from motor planning activity for response generation, which is not captured in the model. We analyze the simulation result that a color cue can increase fidelity even when only a single item is held in

working memory below. We further note that variability of fidelity within each condition was lower in our simulations than in the experimental data. To fully capture the experimental results, the model would likely have to incorporate additional sources of variability such as fluctuations in attention across trials.

Following the analysis in the fMRI study, we fit the activation profiles in all conditions with a Gaussian-like function with variable baseline, separately for the first (6.75 and 9 sec) and second memory period (15.75 and 18 sec). The mean activation profiles and function fits are shown in Figure 6. We used a resampling procedure to determine significance of differences in the fitted parameters between conditions and delay periods. For the first memory period, we found a significantly higher amplitude of the central activation peak in the R1 condition compared with both R2-neutral and R2-valid conditions $(p < .001)$. Conversely, the baseline of the fit was higher

Figure 5. Time course of representational fidelity for target location in different task conditions for the experimental results (adapted from Sprague et al., 2016) and model simulations. Shaded areas indicate 95% confidence interval based on resampling.

in the R2-neutral and R2-valid conditions than in the R1 condition ($p < .001$). No other significant differences between the fitted parameters for different conditions were observed for the first memory period. These findings fully reproduce the observed effects of set size in the fMRI study.

The findings can be explained from the evolution of activation in the neural model and the effects of the reconstruction procedure. The target representation in the R1 condition is stronger due to the color cue that is presented right after stimulus offset in this condition. This raises activation in the whole field for the cued color and, in particular, strengthens the existing activation peak in this field, yielding higher activation for the cued item's location in the reconstruction (in which the fields for different colors are collapsed). In the neural model,

Figure 6. One-dimensional reconstructions over angular space for different task conditions in neural model simulations. Mean activation profiles across trials are shown separately for the first (top row) and second delay period (bottom row) of the task. Red line shows reconstructions, with shaded red area indicating 95% confidence interval based on resampling. Dashed black lines show fitted functions.

the single sustained activation peak during the memory period in the R1 condition is also stronger than the corresponding peaks in the R2 conditions due to lack of mutual inhibition between peaks. The inhibitory interactions implement a form of normalization of total working memory activity in the model. This aspect is consistent with continuous resource models of working memory capacity (Bays, 2014; Bays & Husain, 2008), although we note that the neural field model also incorporates aspects of discrete representations linking them to slot models (Johnson et al., 2014).

In the R2 conditions, the additional sustained peaks for the nontarget item in each trial are reflected in the activation profiles. Nontarget positions are offset from the target position by $\pm 60^{\circ}$, $\pm 120^{\circ}$, or 180° (with some additional random variations), so that the corresponding activation peaks are distributed evenly in orientation space when the reconstructions are aligned on the target position. They contribute therefore to a higher baseline activation in the fitted function. Because the fit amplitude is determined as height of the central activation peak over this baseline, the increased baseline itself also contributes to a reduced amplitude estimate in the reconstructions for the R2 condition.

These effects in the model were confirmed by directly applying the function fits to the field output (summed over both fields of the model), taken at the midpoint of the first delay period. As in the reconstructions, we found a significantly higher amplitude, but lower baseline, in the R1 condition compared with both R2-neutral and R2-valid conditions (all $ps < .001$). The higher baseline component in the R2 conditions was greatly diminished when applying the fits only to the field containing the target item in each trial, confirming that it primarily reflects contributions from nontarget items. The higher amplitude for the R1 condition was still preserved in this case, showing that the activation for the target item is stronger in this condition.

During the second memory period, the same set size effects in the reconstructions were observed when comparing R1 and R2-neutral condition, with higher amplitude ($p < .001$) and lower baseline ($p < .001$) in the R1 condition. In the R2-valid condition, however, target representation amplitude following the informative retrocue is higher than in both the R2-neutral ($p < .001$) and R1 conditions ($p < .001$). These results reproduce analogous findings in the fMRI study. One effect from that study that we did not observe in the simulation results was an increased baseline activation in the R2-valid condition. In fact, we found baseline values in the R2 valid condition that were significantly lower than in the R2-neutral condition ($p < .001$) and not significantly different from the R1 condition ($p = .95$). No further significant differences in parameters across conditions were observed for the second memory periods.

In the neural model, the effects of the retro-cue on peak amplitude in the second memory period are explained by the same mechanisms as the set size effects in the first memory period. The color cue input transiently strengthens the activation peak for the cued item and, by suppressing the sustained peak for the noncued item, removes inhibition from that peak for the second memory period. The color cue also globally raises the activation level (and, to some extent, the output signal derived from it) for the whole field of the matching color. This may, in principle, provide an explanation for the experimentally observed increase in fit baseline for the R2-valid condition compared with the R2-neutral condition. However, in the present model implementation, this effect is outweighed by the decrease in baseline that is brought about by the disappearance of the sustained activation peak for the noncued item.

We again tested these explanations by fitting the field output directly, now at the midpoint of the second delay period. We found the same effects as in the reconstructions when comparing R1 and R2-neutral conditions (all $ps < .001$). For the R2-valid condition, both amplitude and baseline were intermediate between R1 and R2 neutral condition ($p < .001$ for all comparisons). Fit amplitude in this condition did spike during the presentation of the retro-cue but then quickly diminished again in the neural model. In the reconstruction, this transient spike is carried over to the second delay period due to the low-pass filter properties of the hemodynamic response function.

Correlations between Reconstructions and Response Errors

Having demonstrated that the neural model can reproduce both behavioral and reconstruction results, we now analyze interactions between trial-to-trial report performance and reconstruction quality. We divided the trials of each block within each condition into two groups with recall error lower and higher than median recall error in that block, respectively. We then generated reconstructions and function fits for each group and each condition. We found a significantly higher amplitude of the target representation in the low-error group compared with the high-error group for the R2-neutral and R2-valid condition in the second delay period (R2-neutral: mean amplitude 0.058 vs. 0.033 , $p < .001$; R2-valid: mean amplitude 0.095 vs. 0.076, $p = .012$). Similar findings were reported in the experimental study, although a significant effect of error rate on fit amplitude was observed only in the R2-valid condition for the second delay period and in the R2-neutral condition for the first memory period. These results were interpreted as evidence that the reconstruction quality reflects the quality of the working memory representations.

In the neural simulations, these results can be explained by the fact that the high-error group will most likely contain all trials in which the activation peak for the target item collapsed during the delay period as a result of random noise, as well as those trials in which there was significant drift in peak position. For trials in which the activation peak collapsed, the reconstruction will either show no peak or a peak at a new random location (which can form in response to the retro-cue). Both will contribute only to baseline activation in the aligned reconstructions. Trials with high drift of the activation peak will contribute to a central peak in the reconstructions, but this peak will be smeared out when trials are aligned with respect to the stimulus position. Overall, peak amplitude in the aligned reconstructions will then be lower in high-error versus low-error trials.

It should be noted here that the retro-cue in the neural model cannot retroactively restore memory precision. Although the cue does strengthen the sustained activation peak for the cued item, any drift in peak position that occurred before the cue will still be reflected in peak position after the cue. Also, if the activation peak collapsed before the retro cue was given, the spatially uninformative cue can only induce a new peak at a random location. Thus, the interactions between report performance and reconstruction quality and the observed increase in reconstruction quality after the retro-cue do not provide any evidence that a retro-cue actually restores representational precision. The retro-cue may merely reduce further loss of precision after the cue is presented.

Components of the Retro-cue Effect

Using the neural model, we can selectively assess the contribution of different components of the neural representation to the reconstruction quality and its restoration following the retro-cue. Although we cannot tell from simulation results alone whether the components identified here also play a role in the biological neural system, we can make predictions regarding their signatures in reconstructions that could be tested with fMRI data.

As a first component in the full reconstruction, we analyze the effect of the stimulus presentation in the absence of any working memory processes. To this end, we set the weight c_{exc} of excitatory interactions in the neural model to zero. With this modification, the neural population representation in the model still forms peaks of activation in response to external stimulation, but these peaks collapse as soon as the stimuli disappear (i.e., the model does not show any working memory capabilities; Figure 7A).

The time course of reconstruction fidelity for this model in the R2-valid condition is shown in Figure 7B (the time courses for the R1 and R2-neutral conditions are virtually identical in this modified model). During the first half of the trial, the time course of fidelity is similar to those observed in the full model for the R2-valid and R2-neutral condition, but then fidelity decreases and even becomes negative during the second half of the trial. This reflects the shape of the canonical hemodynamic response function, which likewise takes negative values about 12 sec after a pulse of activation. These results suggest that a large part of the early reconstructions are dominated by a sensory response (and possibly attention effects, which we do not capture as a separate component in the model), but it also shows that a working memory component is necessary to account for the positive reconstruction fidelity in the latter part of the trial. The simulation results also confirm that the spatially nonspecific color cue input, which is provided after the first half of the delay period, has no effect on reconstruction fidelity in the absence of sustained activity.

In a second model variant, we assess how removing irrelevant items from working memory contributes to the increase of reconstruction fidelity following an informative retro-cue. In the original model, the retro-cue is implemented as a positive homogeneous input to the neural field corresponding to the cue color, which increases activation levels in this field and leads to the extinction of the activation peak for the uncued item through global inhibitory interactions. As an alternative, we now implement the retro-cue as an inhibitory input to the neural field corresponding to the uncued color (with amplitude c_{forget}), which extinguishes any activation peaks in this field without directly strengthening activation for the cued item (Figure 7C).

Figure 7D shows the time course of reconstruction fidelity of this model variant in the R2-valid condition. Removal of the noncued item leads to an increased fidelity in the second half of the trial compared with the R2-neutral condition (compare to dashed green line). However, the rise in fidelity following the retro-cue is weaker and occurs with longer delay than in the original model. The removal of an irrelevant item thus contributes to the retro-cue effect in the model but does not fully account for it.

To test the direct contribution of the cue input to reconstruction quality in the model, we return to the original model variant but modify the task. Instead of presenting two colored stimuli in the beginning, we only present a single one, which is always the cued item and response target (Figure 7E). This means that the retrocue does not provide any additional information for the task. Nonetheless, we find that the retro-cue significantly increases the reconstruction quality in the model (Figure 7F) in a manner very similar to the retro-cue effect in the original task (dashed blue line). Note that overall reconstruction quality is higher in this condition due to the absence of the nontarget item.

This result can be explained by interaction effects in the neural model. The color cue is emulated as a homogeneous positive input to the neural field. In the absence of any sustained activation, this input would simply raise activation equally over the whole field, which would not produce any change in the fidelity measure (as demonstrated in the model variant without working memory states; Figure 7B). When a sustained peak of activation is present, activation initially also rises homogeneously;

Figure 7. Evolution of activation patterns and fidelity time courses in model simulations for different model and task variants based on the original R2-valid condition. (A, B) Neural model without lateral excitatory interactions. (C, D) Model variant with color cue realized through inhibition of noncued items. (E, F) Task variant with only the target item presented in the sample array. (G, H) Model variant with weak (unreliable) retro-cue input. The field activations are shown for the case of a valid retro-cue; fidelity plots are shown for both valid (blue) and invalid (red) retro-cue. The dashed lines in the fidelity plots show the mean fidelity from the original R2-valid (blue) and R2-neutral condition (green) for comparison. Shaded areas in fidelity plots indicate 95% confidence interval based on resampling.

but as it does, the field output that drives lateral interactions (computed from the activation via a sigmoid function, Equation 2) increases most strongly at the edges of the existing peak. The peak expands further under the influence of local excitation and consequently suppresses activation in the remaining field (as well as the second, noncued field) through global inhibition (Figure 7E). Overall, the concentration of activation at the location of the existing peak is increased, leading to the increase in measured reconstruction fidelity.

We note that, for this simulation, we assumed that the cue would have the same effect as in the original task despite being uninformative. Human observers would likely pay less attention to the cue or ignore it entirely under these conditions, leading to diminished effects on working memory representations. We did not observe any benefit of the retro-cue on behavioral performance in the model (compared with simulations with a single target stimulus without retro-cue; mean response error in both cases 0.41° , $p = .91$). This is due to the fact that behavioral cueing effects in the model are based on biasing the competition between different working memory items, which does not occur in the case of a single item.

Generalization of the Model to Unreliable Retro-cues

The experiment we emulated with the neural model (Sprague et al., 2016) exclusively uses retro-cues with 100% reliability, but many studies on retro-cues use lower reliabilities, such that participants have an incentive to retain uncued items in memory as well (Souza & Oberauer, 2016). Here, we test whether the neural model can be adapted to this scenario. We make a single change to the implementation, namely reducing the strength of the homogeneous boost input that emulates the color cue (amplitude 2.5 compared with 17.5 in the original model; the amplitude for the definitive response cue at the end of the trial is left unchanged). With this setting, the input transiently strengthens the sustained activation for the cued item but does not increase its activation levels to such a degree that the peak for the noncued item will be extinguished (Figure 7G).

We tested the model in trials with either a valid (matching the target color) or invalid retro-cue (matching the nontarget color) provided after the first half of the delay period and an unambiguous response cue indicating the target at the end. The fidelity time course for these simulations is shown in Figure 7H. The valid retrocue causes a small rise in fidelity, whereas the invalid retro-cue causes a faster drop in the representational fidelity of the target compared with the original R2-neutral condition (dashed green line). Nonetheless, even with an invalid retro-cue the fidelity remains above zero throughout the trial and recovers when the response cue is given, indicating that the uncued item is retained in working memory in a majority of trials.

We found a significant effect of cue validity on response errors, with response error lower than in the original R2-neutral condition for valid retro-cues (mean error 0.74°) and higher for invalid retro-cues (1.46°; significantly different based on resampling procedure, $p <$.001). This qualitatively reproduces the most prominent effect of retro-cueing in the literature (see, e.g., Pertzov, Bays, Joseph, & Husain, 2013). The retro-cue effect on performance was driven by a lower rate of peak collapse in the valid than in the invalid retro-cue condition (14.0% vs. 43.5%). We did not find a significant difference in precision for those trials where the peak was sustained (mean response error 0.41° for both conditions, $p = .96$, likely due to the fact that the separate fields for red and blue item do not allow any local interactions between the two activation peaks in the model. Behavioral studies on retro-cue effects have consistently shown a benefit for the probability of reporting the correct item (rather than guessing or reporting the feature of nontarget item), with only some of the studies showing a precision benefit (see Souza & Oberauer, 2016, for a review). We note that our model does not produce any swap errors, which contribute significantly to nontarget responses in behavioral studies. These might potentially be addressed by extending the model with an additional purely spatial memory representation that does not capture binding information (Matthey, Bays, & Dayan, 2015).

DISCUSSION

We have presented a neurodynamic model of retro-cue effects in visual working memory, and we have demonstrated that this model can reproduce behavioral and reconstruction results from an fMRI study, which were interpreted as supporting a latent working memory state (Sprague et al., 2016). The study had found an increase in reconstruction quality after a retro-cue, as well as correlations between reconstruction quality and response error. The authors had argued that these findings provide evidence for a working memory state that is not detectable in the fMRI signal but that can be reactivated by the retro-cue. They proposed that this was likely an activitysilent state, encoded, for example, in changes in synaptic connectivity or sustained subthreshold changes in membrane potential (Stokes, 2015). The neural model presented here does not feature such a latent memory state, relying entirely on sustained neural activity for working memory representations (Wang, 2001). The fact that the model can nonetheless reproduce all key experimental findings refutes the argument for an activitysilent working memory state. Such a state may still exist, but it is not necessary to explain any of the experimental findings from the fMRI study.

We aimed to keep the neural model as simple as possible, making only minimal assumptions about the neural architecture beyond the basic mechanism of sustained activity through self-excitation. In particular, we employed a continuous approximation of the discrete spiking activity in biological neural systems. Previous models of sustained memory activity using continuous firing rates have produced results very similar to more detailed spiking models (Compte et al., 2000; Camperi & Wang, 1998), so we believe that this simplification does not qualitatively alter model behavior. As a further simplification, we did not separately model individual cortical areas or distinguish between sensory and working memory representations. The simulation results suggest that a large portion of the fMRI signal in the experimental study is driven directly by the visual stimuli (which may comprise both purely sensory activity and working memory encoding), but a sustained working memory component is still necessary to fully explain the signal. Spatial attention may also contribute to the fMRI signal and the observed retrocue effect, given that previous behavioral studies have found that a color cue can enhance spatial attention for a memorized item location even if the location is not task relevant (Theeuwes, Kramer, & Irwin, 2011). However, neither the experimental study nor the model presented here investigates the role of attention in this task.

One key assumption we did make in the model is that the working memory representation captures the binding between colors and locations (Treisman, 1996). Binding information is essential to solve the behavioral task (reporting the location of the cued item, rather than randomly reporting the location of either stimulus) but is not reflected in the reconstructions used by Sprague et al. (2016). Following previous neural field models of feature binding in visual working memory (Schneegans et al., 2016; Johnson, Spencer, & Schöner, 2008), we employ a population representation with conjunctive coding. This kind of representation has recently been shown to account for behavioral signatures of binding failures in working memory tasks (Schneegans & Bays, 2017; Matthey et al., 2015). Some of the previous implementations have combined the conjunctive coding with separate feature-specific representation for more efficient representation of individual feature values (Schneegans et al., 2016; Matthey et al., 2015). We omitted such a mechanism here for the sake of simplicity, but we note that some of the neural representations for working memory and attention that contribute to the fMRI signal are likely to be purely spatial and only indirectly interact with representations of stimulus color.

The proposed model constitutes to our knowledge the first neural process model of retro-cue effects. The neurodynamic mechanism employed here integrates several hypotheses about the mechanisms underlying retro-cue effects (Souza & Oberauer, 2016). The cue directly increases activation of the sustained activation peak that reflects the cued item, making use of the conjunctive coding to increase activation in the spatial representation in response to a color cue. This realizes a form of refreshing of the cued item (Rerko & Oberauer, 2013; Chun &

Johnson, 2011). Increasing the activation of one working memory item reduces activation for other items by means of lateral inhibition in the model, consistent with resource models of working memory (Bays, 2014; van den Berg, Shin, Chou, George, & Ma, 2012; Bays, Catalao, & Husain, 2009; Bays & Husain, 2008). For fully reliable retro-cues, this leads to the complete extinction of other working memory items, consistent with the idea that retrocues act through removal of irrelevant items (Souza et al., 2014; Kuo, Stokes, & Nobre, 2012). The model also qualitatively captures effects of less reliable cues, which decrease the chance of forgetting the cued item (through noiseinduced collapse of the sustained activation peak) at the cost of an increased chance of forgetting noncued items.

All performance effects of the retro-cue in the present model are due to protection of the cued item from decay after the retro-cue. This is consistent with previous findings from delayed estimation tasks showing a continuous decrease of response precision with retention interval duration that can be alleviated by a valid retro-cue (Pertzov et al., 2013). This explanation has been questioned by Souza and Oberauer (2016) based on contradictory findings from Gressmann and Janczyk (2016), but these latter findings were based on a change detection task, which may not provide sufficient sensitivity to detect changes in memory precision. Souza and Oberauer (2016) also point to findings that retro-cues increase performance compared with no-cue trials with shorter delay period (matched to the time before the retro-cue; Makovski, Sussman, & Jiang, 2008). A possible cause for this effect is that the retro-cue triggers the retrieval of the cued item without the perceptual interference that may be created by elements of the response display (such as probe stimuli in change detection tasks or a color wheel in delayed estimation tasks; Souza, Rerko, & Oberauer, 2016; Makovski, Watson, Koutstaal, & Jiang, 2010). Accounting for such effects is beyond the scope of the present model.

The retro-cue mechanism in the neural model accounts for the restoration of reconstruction quality for the target item's location that was observed in the fMRI study. Sprague et al. (2016) interpreted this effect of the retro-cue as evidence for an activity-silent working memory state based on the following reasoning: By the time the retro-cue was given, the working memory representation of the memorized location as measured by fMRI reconstruction quality was already degraded to a certain degree; the retro-cue did not provide any spatial information, so it could not have improved the representation of the target's location; thus, the improved reconstruction quality after the retro-cue must have been caused by the reactivation of an activity-silent working memory representation (realized, e.g., through changes in synaptic connectivity) that was not detectable in the fMRI data before the retro-cue.

We argue that there are several problems with this line of reasoning. First, although the color cue does not provide any spatial information by itself, it does allow the selection of a single memorized location if the working memory representation provides information about the binding of colors to locations, as we have argued above. This allows, at the very least, the selective removal of uncued items from working memory. We have demonstrated in model simulations that the selective removal of uncued items produces an increase in reconstruction quality for the cued item using the fidelity measure proposed by Sprague et al. (2016). The reconstruction method does not attempt to estimate memorized color information and thereby loses part of the information that is necessary to explain the effect of the color cue on the spatial representation.

Second, even an entirely uninformative cue can produce an increase in reconstruction quality through the effects of neural interactions in conjunction with sustained activation states. We have shown in the simulations that, even when only a single item is held in working memory, a color cue for that item produces a rise in the fidelity of its reconstruction. The same color cue does not affect fidelity in the absence of sustained working memory activity. In this latter case, the cue only produces a homogeneous rise in activation. But in the presence of a sustained activation peak, the elementary connection pattern of local excitation and surround inhibition in the model transforms this homogeneous input into a specific increase of activation for the existing peak. In a more complex neural architecture with multiple interconnected representations, the combination of a nonspecific input with a sustained activation state may even have much more dramatic effects. Such effects have been employed to drive complex state transitions in neurodynamic models (Schneegans et al., 2016; Richter et al., 2014).

The results of other reconstruction studies may still pose a challenge for the present model. In several experiments, decoding quality was found to fall to chance level for memorized items outside the focus of attention but could be restored at a later time following informative cues or unspecific stimulation (Wolff et al., 2017; Rose et al., 2016). In the neural model, once sustained activity has ceased and the activation peak has collapsed, it cannot be restored by unspecific external stimulation. It is possible, however, that the experimental studies merely failed to detect the signatures of weak neural activity that was sustained throughout the memory period. This might occur because the relationship between firing rate and BOLD/EEG signal is less straightforward than the direct linear relationship assumed here (e.g., Logothetis, Pauls, Augath, Trinath, & Oeltermann, 2001). If this is the case, mechanisms similar to the ones described in this study may explain how weak sustained activity can be amplified and become detectable again in response to unspecific input to the neural system.

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